Quiz  $\mathbf{2}$ 

Name: \_\_\_\_\_

Time Begun:	
Time Ended:	

Friday September 24 Prof. Ron Buckmire

**Topic** : Practice With Bifurcations

The idea behind this quiz is to provide you with an opportunity to illustrate your understanding of bifurcations in first-order ordinary differential equations.

## Reality Check:

EXPECTED SCORE : \_\_\_\_/10

ACTUAL SCORE : \_\_\_\_\_/10

## Instructions:

- 0. Please look for a hint on this quiz posted to faculty.oxy.edu/ron/math/341/10/
- 1. Once you open the quiz, you have **30 minutes** to complete, please record your start time and end time at the top of this sheet.
- 2. You may use the book or any of your class notes. You must work alone.
- 3. If you use your own paper, please staple it to the quiz before coming to class. If you don't have a stapler, buy one. QUIZZES WITH UNSTAPLED SHEETS WILL NOT BE GRADED.
- 4. After completing the quiz, sign the pledge below stating on your honor that you have adhered to these rules.
- 5. Your solutions must have enough details such that an impartial observer can read your work and determine HOW you came up with your solution.
- 6. Relax and enjoy...
- 7. This quiz is due on Monday September 27, in class. NO LATE OR UNSTAPLED QUIZZES WILL BE ACCEPTED.

**Pledge:** I, \_\_\_\_\_\_, pledge my honor as a human being and Occidental student, that I have followed all the rules above to the letter and in spirit.

DIFFERENTIAL EQUATIONS

Math 341 Fall 2010

## SHOW ALL YOUR WORK

Quiz  $\mathbf{Two}$ 

1. Consider the following one-parameter family of nonlinear, first-order, autonomous differential equations where  $\alpha$  is a known real parameter value

$$\frac{dy}{dx} = y^2 - \alpha y + 1.$$

(a) 2 points. Show that this DE has no equilibrium values when  $|\alpha| < 2$ .

(b) 2 points. For what values of  $\alpha$  will the DE have exactly one equilibrium value? Classify the equilibrium point (as node, source or sink) in this case and write down the constant solution.

(c) 4 points. Show that when  $|\alpha| > 2$  the DE has exactly one stable equilibrium value (sink) and one unstable equilibrium value (source). Show work that supports your classification of the equilibria, and sketch a phase line for a representative value of  $\alpha$ .

(d) 2 points. Use your answers from above to sketch the bifurcation diagram for the given DE. Clearly indicate where sources, sinks and nodes occur.