Quiz 9	$Linear\ Systems$
Name:	<u> </u>
Date:	Friday April 11 Ron Buckmire
Topic: Orthogonality and Orthogonal Comple	ements
The idea behind this quiz is for you to indicate you complements.	ur understanding of orthogonality and orthogonal
Reality Check:	
EXPECTED SCORE :/10	ACTUAL SCORE :/10
Instructions:	
0. Please look for a hint on this quiz posted to fac	ulty.oxy.edu/ron/math/214/08/
1. Once you open the quiz, you have 30 minutes time at the top of this sheet.	to complete, please record your start time and end
2. You may use the book or any of your class notes	. You must work alone.
3. If you use your own paper, please staple it to the stapler, buy one. QUIZZES WITH UNSTAPLE.	
4. After completing the quiz, sign the pledge below these rules.	w stating on your honor that you have adhered to
5. Your solutions must have enough details such t determine HOW you came up with your solution	- v
6. Relax and enjoy	
7. This quiz is due on Monday April 14, in class BE ACCEPTED.	ass. NO LATE OR UNSTAPLED QUIZZES WILL
Pledge: I,, pledge my	honor as a human being and Occidental student,

Goal: To project $\vec{v} = (1, 5, 0)$ onto the orthogonal complement (denoted by \mathcal{W}^{\perp}) of the plane x - y + 3z = 0 (denoted by \mathcal{W}) in \mathbb{R}^3 .

- (a) (2 points). If the set of points (x, y, z) in \mathbb{R}^3 are represented as the vector $\vec{x} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$, the set of points on the plane x y + 3z = 0 can be represented as the vectors found in the nullspace of what matrix? (Re-write x y + 3z = 0 as $A\vec{x} = 0$ and identify A and list its matrix dimensions).
- (b) (2 points). Since the plane x y + 3z = 0 is a 2-dimensional object and given that the rank of the matrix A is 1, write down a basis for null(A) which contains 2 vectors.

- (c) (2 points). Using the Rank Theorem, write down a basis for the orthogonal complement of the nullspace of A. (HINT: what is the dimension of this orthogonal complement?)
- (d) (2 points). Your answer in (c) is a basis for the orthogonal complement of the nullspace of A, in other words \mathcal{W}^{\perp} . Find $\vec{w}_1 = \operatorname{proj}_{\mathcal{W}^{\perp}}(\vec{v})$, where $\vec{v} = \begin{bmatrix} 1 \\ 5 \\ 0 \end{bmatrix}$.
- (e) (2 points). Use your answer to find $\vec{w}_2 = \text{proj}_{\mathcal{W}}(\vec{v})$. What (two) properties do \vec{w}_1 and \vec{w}_2 have that you can check to confirm your values of \vec{w}_1 and \vec{w}_2 are correct?