Quiz 8

Linear Systems

Date:	
Time Begun:	
Time Ended:	

Friday April 4 Ron Buckmire

Topic : Diagonalization of a Matrix and its Implications for Matrix Exponentiation

The idea behind this quiz is for you to indicate your understanding of the application of finding eigenvalues and eigenvectors associated with a matrix to computing steady state asymptotic values of the matrix.

Reality Check:

EXPECTED SCORE : ____/10

ACTUAL SCORE : _____/10

Instructions:

- 0. Please look for a hint on this quiz posted to faculty.oxy.edu/ron/math/214/08/
- 1. Once you open the quiz, you have **30 minutes** to complete, please record your start time and end time at the top of this sheet.
- 2. You may use the book or any of your class notes. You must work alone.
- 3. If you use your own paper, please staple it to the quiz before coming to class. If you don't have a stapler, buy one. QUIZZES WITH UNSTAPLED SHEETS WILL NOT BE GRADED.
- 4. After completing the quiz, sign the pledge below stating on your honor that you have adhered to these rules.
- 5. Your solutions must have enough details such that an impartial observer can read your work and determine HOW you came up with your solution.
- 6. Relax and enjoy...
- 7. This quiz is due on Monday April 7, in class. NO LATE OR UNSTAPLED QUIZZES WILL BE ACCEPTED.

Pledge: I, _____, pledge my honor as a human being and Occidental student, that I have followed all the rules above to the letter and in spirit.

Math 214 Spring 2008

SHOW ALL YOUR WORK

1. Consider the matrix $A = \begin{bmatrix} 1/2 & 1/2 \\ 1 & 0 \end{bmatrix}$. We want to obtain a value for $A^{\infty} = \lim_{n \to \infty} A^n$.

a. (4 points). Find the eigenvalues and eigenvectors of A.

b. (2 points) Show that $AS = S\Lambda$ or $A = S\Lambda S^{-1}$, where the columns of S are formed by the eigenvectors of A and Λ is a diagonal matrix with the eigenvalues of A along the diagonal and zeroes elsewhere.

c. (2 points). Compute $A^n = S\Lambda^n S^{-1}$.

d. (2 points). Use your answer from **c** to show that $A^{\infty} = \begin{bmatrix} 2/3 & 1/3 \\ 2/3 & 1/3 \end{bmatrix}$.