Class 13: Friday February 23 Learning the Anti-differentiation Process

$\overline{\text{GroupWork}}$

Look at the following table and try and fill in the missing functions. Do you notice any patterns?

g'(x)	g(x)
	$\cos(3x)$
$\sin(2x)$	
$\sin(7x)$	
$\sin(\frac{1}{6}x)$	
$\sin(Ax)$	
$\sin(Ax+B)$	
$\cos(2x)$	
$\cos(Ax+B)$	
$(Ax+B)^{25}$	
f(x)	$\int f(x)dx$

Math 120

The anti-derivatives on the other side can all be calculated by the "Guess and Check" Method. That is, given a function f(x) you are supposed to anti-differentiate, you pick a function F(x) that when you differentiate you get something which looks very close to f(x).

In the examples in the table, all the functions looked like f(Ax + B). In fact, they really looked like g'(Ax + B). Can you use your experience from the table to evaluate the following integral?

$$\int g'(Ax+B) \ dx =$$

Let us check the answer by differentiating our guess.

Q: What DERIVATIVE rule do we have to use?

Derivative of a Composite Function

Suppose h(x) = g(p(x)). Then

$$\frac{dh}{dx} = h'(x) = g'(p(x)) \cdot p'(x).$$

The derivative of a composite function h(x) is the product of the derivatives of the outside and inside functions. The derivative of the outside function must be evaluated at the inside function.

ANTI-Derivative of a Composite Function

We can use The Chain Rule combined with the Fundamental Theorem of Calculus to evaluate the following integrals

1.
$$\int g'(p(x))p'(x)dx$$

$$2. \int \sin(x^2) 2x dx$$

3.
$$\int \cos(e^x)e^x dx$$

4.
$$\int \cos(e^x) dx$$