

EXPLAIN EVERY ANSWER!

1. Use the different functions $f(x) = 3^{(x^2)}$ and $g(x) = (3^x)^2$ for all parts of this quiz.

a. (4 points). Write $f(x)$ and $g(x)$ as the composition of two functions of your choosing, p and q , such that $f = p \circ q$ and $g = q \circ p$. **Confirm** that your choice for p and q satisfy the condition that $q(p(x)) = g(x)$ and $p(q(x)) = f(x)$.

$$f(x) = 3^{(x^2)} = p(q(x)) \quad \text{where } p(u) = 3^u, u = x^2 = q(x)$$

$$(p \circ q)(x) = 3^{q(x)} = 3^{x^2}$$

$$g(x) = (3^x)^2 = q(p(x)) = q(3^x) = (3^x)^2$$

b. (4 points). Find the derivatives $f'(x)$ and $g'(x)$.

$$[3^{(x^2)}]' = f'(x) = 3^{x^2} \cdot \ln 3 \cdot 2x = p'(q(x)) \cdot q'(x)$$

$$[(3^x)^2]' = g'(x) = 2 \cdot 3^x \cdot \ln 3 \cdot 3^x = q'(p(x)) \cdot p'(x)$$

$$p'(u) = 3^u \ln 3$$

$$q'(x) = 2 \cdot x$$

c. (2 points). Evaluate $f'(1)$ and $g'(1)$.

$$f'(1) = 3^1 \cdot \ln 3 \cdot 2 = 6 \ln 3$$

$$g'(1) = 2 \cdot 3^1 \cdot \ln 3 \cdot 3 = 18 \ln 3$$

$$f'(1) \neq g'(1)$$