

Class 23 HW SOLUTIONS to selected problems. Math 110, Fall 98  
Was due 11/02/98: HH, section 4.7: 1, 5, 7, 13, 18; CANCEL #11.

1.  $x^2 + y^2 = \sqrt{7}$ .

Apply  $d/dx$  to both sides:  $2x + 2yy' = 0$ .

Now solve for  $y'$ :  $2yy' = -2x$ ,  $y' = x/y$ .

3.  $\ln x + \ln(y^2) = 3$ , so  $1/x + (1/y^2)2yy' = 0$ ,  
so  $(1/y^2)2yy' = -1/x$ , so  $(2/y)y' = -1/x$ , so  $y' = -y/(2x)$ .

7. We did this in detail in class. See class notes.

11. Cancelled.

18. (a)  $x^2 + y^2 = 25$ . So  $2x + 2yy' = 0$ .

Plugging in  $x = 4$  into the equation of the circle (not its derivative) gives  
 $y = 3$  or  $y = -3$ .

Plugging in the point  $(4,3)$  into the implicit equation for the derivative, we  
get:

$2(4) + 2(3)y' = 0$ . Solve this to get:  $y' = -3/4$ .

A similar procedure for the point  $(4,-3)$  gives  $y' = 3/4$ .

Now use the point-slope formula to find equations for the two lines.

Parts (b) and (c) are straightforward. (See class notes.)